## **Review Problems for Midterm III**

- (1) Find the general solution of the following differential equations.
  - (a)  $y^{(6)}(t) + 64y(t) = 0$ .
  - (b)  $y^{(3)}(t) + 3y^{(2)}(t) + 2y'(t) = 0.$
  - (c)  $y^{(4)}(t) 8y^{(2)}(t) + 16y = 0$ .
  - (d)  $y^{(6)}(t) + 2y^{(3)}(t) + y(t) = 0.$
  - (e)  $(D^2 4D + 13)^2(D 2)^2y(t) = 0.$
- (2) Use the method of Annihilators to find the form of particular solution of the following problems.
  - (a)  $(D^3 2D^2 + D)y = t + \cos(t) + t\sin(t) + t^2e^t$ .
  - (b)  $(D^3 + D)y = t + \cos(t) + t\sin(t) + t^2e^t$ .
  - (c)  $y''(t) + 2y'(t) + 2y(t) = 3te^{-t}\cos(t)$ .
- (3) Use Laplace's transform to find the solution of the following initial value problems.
  - (a)  $y^{(3)}(t) 3y^{(2)}(t) + 2y'(t) = e^{4t}$  with y(0) = 1, y'(0) = 0 and y''(0) = 0.
  - (b)  $y''(t) + y(t) = \sin(2t)$  with y(0) = 0, y'(0) = 0.
  - (c) y''(t) + 4y = g(t) with y(0) = 0 and y'(0) = 0 where

$$g(t) = \begin{cases} 0, & 0 \le t < 2, \\ 3(t-2), & 2 \le t < 4, \\ 6, & 4 \le t. \end{cases}$$

(d) y''(t) + 4y'(t) + 4y = g(t) with y(0) = 0 and y'(0) = 0 where

$$g(t) = \begin{cases} 0, & 0 \le t < 2, \\ 3(t-2), & 2 \le t < 4, \\ 6, & 4 \le t. \end{cases}$$

(e) y''(t) + 4y'(t) + 5y = g(t) with y(0) = 0 and y'(0) = 0 where

$$g(t) = \begin{cases} 0, & 0 \le t < 2, \\ 1, & 2 \le t < 4, \\ 0, & 4 \le t. \end{cases}$$

- (f)  $y''(t) + 5y'(t) + 4y(t) = \delta(t-2)$ , with y(0) = 1 and y'(0) = 1.
- (g)  $y''(t) + 4y'(t) + 5y(t) = \delta(t-2)$ , with y(0) = 0 and y'(0) = 0.
- (h)  $y''(t) 4y'(t) + 4y(t) = \delta(t-2)$ , with y(0) = 0 and y'(0) = 0.
- (4) Express the solution of the given initial value problem in terms of the convolution integral.
  - (a)  $y''(t) + 4y'(t) + 5y(t) = e^{2t}\cos(t)$ , with y(0) = 0 and y'(0) = 0.
  - (b)  $y''(t) 2y'(t) + y(t) = te^t$ , with y(0) = 0 and y'(0) = 0.
  - (c)  $y''(t) 3y'(t) + 2y(t) = te^t + te^{2t}$ , with y(0) = 0 and y'(0) = 0.