

Only nongraphing calculators are allowed. Answer questions 1 to 14 AND EITHER question 15 OR 16 not both. The exam is 2 hours and 200 points are possible. The value of each question is indicated in the left margin.

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Problem	Points	Score
1*	15	
2*	18	
3	12	
4	10	
5*	10	
6	10	
7	10	
8*	21	
9	10	
10*	12	
11	14	
12	18	
13	14	
14	14	
15†	12	
16†	12	
TOTAL	200	

\* Common Assessment Questions      †Either 15 or 16

1. Evaluate the limit, if it exists.

(15)

(a)  $\lim_{x \rightarrow 5} \frac{x^2 - 25}{x^2 - 3x - 10}$

(b)  $\lim_{t \rightarrow -3} \frac{2t}{(t + 3)^2}$

(c)  $\lim_{x \rightarrow 8^-} \frac{|x - 8|}{x - 8}$

2. Differentiate the function.

(18)

(a)  $f(x) = \frac{x^3 + 4x^2}{x^4 + 11}$

(b)  $g(x) = x \tan 5x$

(c)  $g(x) = \sin(x^3) + \sin^2 x$

3. Find  $f'(x)$  from first principles, that is directly from *the definition of a derivative* ( $\lim_{h \rightarrow 0} (f(x+h) - f(x))/h$ ) when

$$f(x) = \sqrt{x-1}.$$

4. If  $f(x) = \sqrt{x}$  and  $g(x) = \sin x$ , find the functions  $f \circ g$ ,  $g \circ f$  and  $g \circ g$  and their domains.

(10)

5. Find an equation for the tangent line to the curve  $y = x\sqrt{x+2}$  at  $(2,4)$ .

(10)

6. Find  $dy/dx$  by implicit differentiation.  $y^3 - 5x^2y = -32$ .

(10)

7. A rock, thrown vertically from 2 m above the surface of the moon with an initial velocity of 16 m/sec, reaches a height of  $s = 2 + 16t - 0.8t^2$  m in  $t$  seconds.

(10)

(a) Find the velocity of the rock after  $t$  seconds.

(b) How high does the rock go?

8. Evaluate the integral.

(21)

(a)  $\int \frac{4x^6 + 3\sqrt{x}}{2x^3} dx$

(b)  $\int \frac{4x^2}{\sqrt{9+x^3}} dx$

(c)  $\int_{\pi/12}^{\pi/9} \sec^2 3\theta \, d\theta$

(10) 9. Find the *derivative* the function  $g(x) = \int_1^{\sqrt{x}} \frac{1}{\sqrt{1+t^4}} \, dt$ .

(12) 10. Find the absolute maximum and minimum of  $f(x) = 3x^4 + 2x^3$ , on the closed interval  $-1 \leq x \leq 1$ .

11. Gravel is being dumped from a conveyor belt at a rate of  $2 \text{ m}^3/\text{min}$  onto a dock. It forms a pile in the shape of a cone whose base diameter and height are always equal. How fast is the height of the pile increasing when the pile is 3 m high? (The volume of a cone of height  $h$  and base *radius*  $r$  is  $\frac{\pi}{3}r^2h$ .)

(14)

12. Find the area of the region enclosed by the curve  $y = 4 - x^2$  and the  $x$ -axis,

(14)

13. Let  $f(x) = x^4 + x^3$

(18)

- (a) Find the intervals of increase or decrease.
- (b) Find the local maximum and minimum values.
- (c) Find the intervals of concavity and the inflection points.
- (d) Use the information from parts (a), (b) and (c) to sketch the graph



14. Find two positive numbers  $x$  and  $y$  so that  $x + 4y = 1000$  and  $xy$  is as large as possible.

(14)

Instructions: Do EITHER question 15 or 16 but not both. If you attempt both then indicate which is to be graded.

15. Use Newton's method and initial approximation  $x_1 = 1$  to find  $x_3$ , the third approximation of the root of the equation and  $x^3 + x - 1 = 0$ .

(12)

16. A particle moving along a line has velocity  $v(t) = t^2 - t$  (in meters per second) Find (a) the displacement and (b) the distance traveled by the particle  $0 \leq t \leq 3$ .

(12)