

$$\underline{17} \quad 2x + \ln y = x^4 y^3$$

$$\frac{d}{dx}(2x) + \frac{d}{dx}(\ln y) = \frac{d}{dx}(x^4 y^3)$$

$$\Rightarrow 2 + \frac{1}{y} \frac{dy}{dx} = x^4 \frac{d}{dx}(y^3) + y^3 \frac{d}{dx}(x^4)$$

$$\Rightarrow 2 + \frac{1}{y} \frac{dy}{dx} = x^4 \cdot 3y^2 \frac{dy}{dx} + y^3 \cdot 4x^3$$

$$\Rightarrow \frac{1}{y} \frac{dy}{dx} - 3x^4 y^2 \frac{dy}{dx} = 4y^3 x^3 - 2$$

$$\Rightarrow \frac{dy}{dx} \left[\frac{1}{y} - 3x^4 y^2 \right] = \underline{4x^3 y^3 - 2}$$

$$\Rightarrow \boxed{\frac{dy}{dx} = \frac{4x^3 y^3 - 2}{\frac{1}{y} - 3x^4 y^2}}$$

$$\underline{18} \quad y^3 + xy^2 - 5 = x + 3y^2, \quad x=3$$

$$\text{Put } x=3, \quad y^3 + 3y^2 - 5 = 3 + 3y^2$$

$$\Rightarrow y^3 = 8$$

$$\Rightarrow y = 2$$

∴ The point is (3, 2)

Find $\frac{dy}{dx}$

$$\frac{d(y^3)}{dx} + \frac{d(xy^2)}{dx} - \frac{d(5)}{dx} = \frac{d(x)}{dx} + \frac{d(3y^2)}{dx}$$

$$3y^2 \frac{dy}{dx} + x \frac{d(y^2)}{dx} + y^2 = 1 + 6y \frac{dy}{dx}$$

$$3y^2 \frac{dy}{dx} + 2xy \frac{dy}{dx} + y^2 = 1 + 6y \frac{dy}{dx}$$

$$\frac{dy}{dx} [3y^2 - 2xy - 6y] = 1 - y^2$$

$$\frac{dy}{dx} = \frac{1 - y^2}{3y^2 - 2xy - 6y}$$

$$\therefore \frac{dy}{dx} \Big|_{(3,2)} = \frac{1 - 4}{3 \cdot 4 - 12 - 12} = \frac{-3}{-12} = \frac{1}{4}$$

$$(y-2) = \frac{1}{4}(x-3)$$

$$\Rightarrow \boxed{y = \frac{x}{4} + \frac{5}{4}}$$