

18 $y = 4x + 12$, $y = x^2$

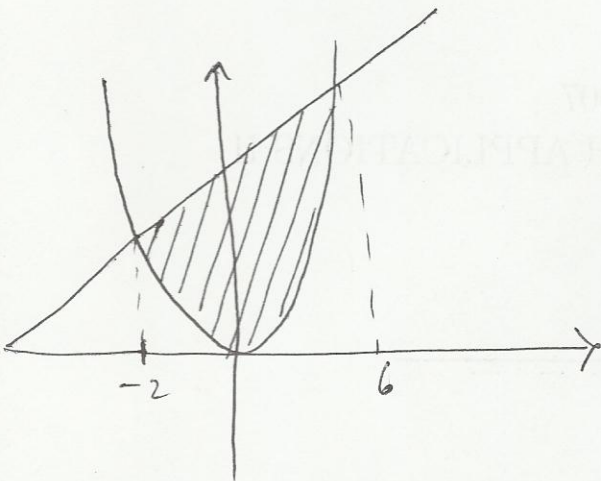
Where do they intersect?

$$4x + 12 = x^2$$

$$x^2 - 4x - 12 = 0$$

$$(x - 6)(x + 2) = 0$$

$$x = 6, -2$$



Find the area of the shaded region

$$= \int_{-2}^6 (4x + 12) - x^2 dx$$

$$= \int_{-2}^6 4x dx + \int_{-2}^6 12 dx - \int_{-2}^6 x^2 dx$$

$$= 2x^2 \Big|_{-2}^6 + 12x \Big|_{-2}^6 - \frac{x^3}{3} \Big|_{-2}^6$$

$$= 2 \cdot 6^2 - 2 \cdot (-2)^2 + 12 \cdot 6 - 12(-2) - \left[\frac{6^3}{3} - \frac{(-2)^3}{3} \right]$$

$$= (72 - 8) + (72 + 24) - \left(72 + \frac{8}{3} \right)$$

$$= 64 + 96 - \frac{224}{3}$$

$$= 160 - \frac{224}{3}$$

$$= \frac{256}{3} = \boxed{85.33}$$