

Sample Questions for MATH 1270 for Exam 3, Spring 2010
March 26, 2011

1. Evaluate

$$\int 9x e^{4x} dx$$

2. Evaluate

$$\int 10x \ln(2x) dx$$

3. Evaluate

$$\int x \sqrt[3]{x+3} dx$$

4. Find the average value of the function on the given interval.

$$f(x) = e^{x/3}, \quad [1, 2]$$

5. Find the average value of the function on the given interval.

$$f(x) = \sqrt{x+1}, \quad [0, 8]$$

6. The function $f(x) = 600$ represents the rate of flow of money in dollars per year. Assume a 20-year period at 4% compounded continuously. Find (a) the present value, and (b) the accumulated amount of money flow at $t = 20$.

7. The function $f(x) = 1500e^{0.02x}$ represents the rate of flow of money in dollars per year. Assume a 15-year period at 4% compounded continuously. Find (a) the present value, and (b) the accumulated amount of money flow at $t = 15$.

8. Find the area, if it is finite, of the region under the graph of $y = \frac{5}{2x^2}$ over the interval $[2, \infty)$.

9. Determine whether the integral

$$\int_{-\infty}^{-5} \frac{4}{x^4} dx$$

converges or diverges, and find the value if it converges.

10. Find the area between the graph of $f(x) = \frac{8}{x-4}$ and the x -axis over the interval $(-\infty, 0]$, if possible.

11. If labor (x) costs \$256 per unit, materials (y) cost \$122 per unit, and capital (z) costs \$84 per unit, write a function for the total cost.

12. For the function $f(x, y) = \sqrt{y^2 + 4x^2}$, find $f(2, -3)$, $f(-5, -5)$ and $f(0, 6)$.

13. For the function $z = f(x, y) = -4x^3 - 6y^2 + 3xy$, find $\frac{\partial z}{\partial x}$, $\frac{\partial z}{\partial y}$, $f_x(4, 0)$, and $f_y(4, 0)$.
14. For the function $z = f(x, y) = \ln |9x^4 + 5x^2y^2|$, find $f_x(x, y)$ and $f_y(x, y)$. Then find $f_x(2, -1)$ and $f_y(-4, 3)$.
15. Find the four second order partial derivatives f_{xx} , f_{yy} , f_{xy} , f_{yx} for

$$f(x, y) = 8x^5y^6 + 7x^8y^4$$

16. Find the local maxima, local minima, and the saddle points of the given function.

$$f(x, y) = x^2 - 6xy + y^2 + 16y + 7$$

17. Find all local extrema for the function

$$f(x, y) = 4y^4 - 32y^2 + 8x^2 - 16$$

18. Use the echelon method to solve the system of equations.

$$4x - 2y + 5z = 72$$

$$5x - 4y - 4z = 2$$

$$x - y + 5z = 46$$

19. Solve the system of equations by setting up an augmented matrix and using the Gauss-Jordan Method.

$$x + 2y - z = 2$$

$$2x + z = 5$$

$$y - 3z = -7$$

20. Solve the system of equations in Question # 19 by finding and using the inverse of the coefficient matrix.