

MATH 1270 Sec 005, 007
CALCULUS FOR THE BUSINESS WITH APPLICATIONS II
QUIZ 2
January 31, 2011

Name (Last, First) _____

1. Find the absolute extrema, if they exist as well as all values of x where they occur.

$$f(x) = x^3 - 3x^2 - 24x + 5, \quad [-3, 6]$$

$f'(x) = 3x^2 - 6x - 24$. Set $f'(x) = 0$ and solve for x .

$$3x^2 - 6x - 24 = 0$$

$$x^2 - 2x - 8 = 0$$

$$(x - 4)(x + 2) = 0$$

$$x = -2, 4.$$

$f'(x)$ is defined everywhere. Therefore the values of x we need to check for maximum/minimum are $-2, 4$ and then endpoints of the intervals $-3, 6$.

$$f(-2) = 33, f(4) = -75, f(-3) = 23, f(6) = -31.$$

Therefore absolute maximum is attained at -2 and the absolute maximum is 33 . Absolute minimum is attained at 4 and the absolute minimum is -75 .

2. Suppose 100,000 lamps are to be manufactured annually. It costs \$1 to store a lamp for 1 year, and it costs \$500 to set up the factory to produce a batch of lamps. Find the number of lamps to produce in each batch.

$$M = 100,000$$

$$f = 500$$

$$k = 1$$

$$\text{Therefore } q = \sqrt{\frac{2Mf}{k}} = \sqrt{\frac{2 \cdot 100,000 \cdot 500}{1}} = 10,000$$