MATH 1850 Sec 001 SINGLE VARIABLE CALCULUS I

QUIZ 9
April 11, 2013


1. Use finite approximation to estimate the area under the graph $f(x)=2 x^{2}$ and above the $x$-axis from $x_{0}=0$ to $x_{n}=12$ using
(a) a lower sum with 4 rectangles of equal width.

$$
\begin{aligned}
& \Delta x=\frac{12-0}{4}=3 \\
& A_{1}=2 \cdot 0^{2} \cdot 3=0 \\
& A_{2}=2 \cdot 3^{2} \cdot 3=54 \\
& A_{3}=2 \cdot 6^{2} \cdot 3=216 \\
& A_{4}=2 \cdot 9^{2} \cdot 3=\frac{486}{756}
\end{aligned}
$$

2. Do the previous problem by taking an upper sum with 6 rectangles of equal width.

$$
\begin{aligned}
& \Delta x=\frac{12-0}{6}=2 \\
& A_{1}=2 \cdot 2^{2} \cdot 2=16 \\
& A_{2}=2 \cdot 4^{2} \cdot 2=64 \\
& A_{3}=2 \cdot 6^{2} \cdot 2=144 \\
& A_{4}=2 \cdot 8^{2} \cdot 2=256 \\
& A_{5}=2 \cdot 10^{2} \cdot 2=400 \\
& A_{6}=2 \cdot 12^{2} \cdot 2=\frac{576}{1456}
\end{aligned}
$$

