

p. 215

$$5. \frac{1}{2}f(-1) + \frac{1}{2}f(-.4) + \frac{1}{2}f(.2) + \frac{1}{2}f(1) \\ = \frac{1}{2}(-1 - .064 + .008 + 1) = \frac{1}{2}(-.056) = \textcircled{-.028}$$

$$6. \frac{1}{2}f(-2) + \frac{1}{2}f(-1.5) + .3f(-1) + .3f(-.7) + .4f(-.4) \\ = \frac{1}{2}(2) + \frac{1}{2}(-.75) + .3(0) + .3(-.21) + .4(-.24) \\ = 1 + .375 + 0 - .063 - .096 = 1.375 - 1.590 \\ = \textcircled{-.215}$$

8c. S is from -3 to 3 so each rectangle has base 1

$$\text{Midpoint approx is: } 1(f(-2.5) + f(-1.5) + f(-.5) + f(.5) + f(1.5) + f(2.5)) \\ = 1(1.5 + 0 + -1 + -1.75 + 1 + 1) \\ = 1(-1.75) = -1.75$$

$$15. \int_0^{\pi} x \sin x \, dx$$

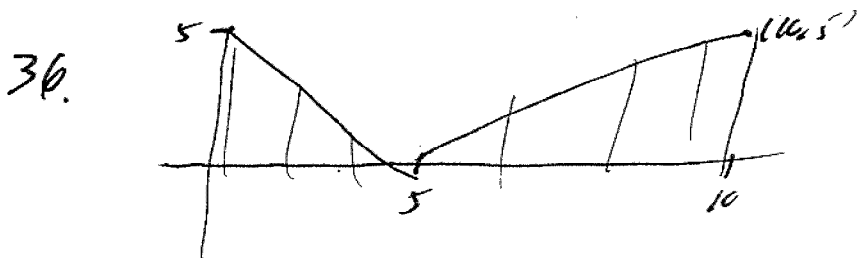
$$16. \int_1^5 \frac{x}{1+x} \, dx$$

$$17. \int_1^2 \sqrt{2x+x^2} \, dx$$

$$18. \int_0^2 4 - 3x^2 + 6x^5 \, dx$$

30. a. 4 b. $\frac{1}{2} \pi \cdot 4 = (2\pi)$ c. $4 - 2\pi + \frac{1}{2} = (\frac{9}{2} - 2\pi)$

32. $\int_{-2}^2 \sqrt{4-x^2} dx$  area (2π)



$\int_0^{10} |x-5| dx = \frac{1}{2} \cdot 5 \cdot 5 + \frac{1}{2} \cdot 5 \cdot 5 = 25$

37. $(-\frac{38}{3})$

38. 0

39. $\int_{-1}^5 f(x) dx$

40. 8.4

41. $(\frac{1}{2}) = 74 + 48$

p. 225

$$4. \int_{-2}^0 4\sqrt{5-u^3+u^2} du = \left. \frac{1}{6} u^6 - \frac{4}{4} u^4 + \frac{1}{3} u^3 \right|_{-2}^0$$

$$= 0 - \left(\frac{64}{6} - 4 - \frac{8}{3} \right) = -\frac{32}{3} - \frac{12}{3} - \frac{8}{3} = \boxed{-\frac{52}{3}}$$

$$-6. \int_1^8 x^{1/3} dx = \left. \frac{3}{4} x^{4/3} \right|_1^8 = \frac{3}{4} \cdot 16 - \frac{3}{4} \cdot 1 = \boxed{\frac{45}{4}}$$

$$11. \int_{-2}^{-1} 4y^3 + 2y^{-3} dy = \left. \frac{4}{4} y^4 - y^{-2} \right|_{-2}^{-1} = (1 - 1) - (16 - \frac{1}{4})$$

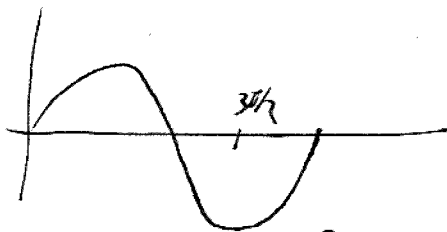
$$= \boxed{-15\frac{3}{4}}$$

$$17. \int_{\pi}^{2\pi} \csc^2 \theta d\theta = \left. -\cot \theta \right|_{\pi}^{2\pi} = 0 - 0 = 0$$

$\csc^2 \theta = \frac{1}{\sin^2 \theta}$ ME at $\theta = \pi, 2\pi$

$$20. \int_0^9 \sqrt{t} dt = \left. \frac{2}{3} \sqrt{t} t^{3/2} \right|_0^9 = \frac{2}{3} \sqrt{t} \cdot 27 - 0 = \boxed{\frac{54\sqrt{2}}{3}}$$

28.



$$\int_0^{3\pi/2} |\sin x| dx = \int_0^{\pi} \sin x dx + \int_{\pi}^{3\pi/2} \sin x dx$$

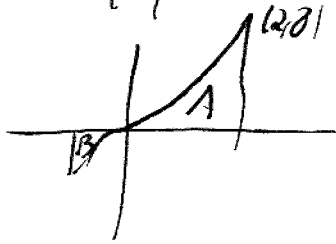
$$= -\cos x \Big|_0^{\pi} + \cos x \Big|_{\pi}^{3\pi/2}$$

$$= -(-1 - 1) + (0 - -1)$$

$$= 2 + 1 = \boxed{3}$$

29. $\frac{1}{x^2}$ is not cont on $[1, 3]$

$$35. \int_{-1}^2 x^3 dx = \frac{x^4}{4} \Big|_{-1}^2 = \frac{16}{4} - \frac{1}{4} = \frac{15}{4}$$



it is area A - area B

$$37. F(x) = \sqrt{x^2+1} + C \quad F'(x) = \frac{x}{\sqrt{x^2+1}} \quad \text{so}$$

$$\int \frac{x}{\sqrt{x^2+1}} dx = \sqrt{x^2+1} + C$$

$$38. F(x) = x \sin x + \cos x + C \quad F'(x) = x \cos x + \sin x - \sin x \\ = x \cos x$$

so

$$\int x \cos x dx = x \sin x + \cos x + C$$

0.241

$$1. \int \cos 3x \, dx = \boxed{\frac{1}{3} \sin(3x) + C}$$

$$2. \int x(4+x^2)^{10} \, dx \quad u = x^2 + 4 \quad du = 2x \, dx \\ = \int \frac{1}{2} u^{10} \, du = \frac{1}{22} u^{11} + C = \boxed{\frac{1}{22} (4+x^2)^{11} + C}$$

$$3. \int x^2 \sqrt{x^3+1} \, dx \quad u = x^3+1 \quad du = 3x^2 \, dx \\ = \int \frac{1}{3} \sqrt{u} \, du = \frac{2}{9} u^{3/2} + C = \boxed{\frac{2}{9} (x^3+1)^{3/2} + C}$$

$$4. \int \frac{\sin \sqrt{x}}{\sqrt{x}} \, dx \quad u = \sqrt{x} \quad du = \frac{1}{2\sqrt{x}} \, dx \\ = \int 2 \sin u \, du = -2 \cos u + C = \boxed{-2 \cos \sqrt{x} + C} \\ = \boxed{-2 \cos(\sqrt{x}) + C}$$

$$5. \int \frac{4}{(1+2x)^3} \, dx \quad u = 1+2x \quad du = 2 \, dx \\ = \int \frac{2}{u^3} \, du = \int 2u^{-3} \, du = -u^{-2} + C = \boxed{\frac{-1}{(1+2x)^2} + C}$$

$$6. \int \cos^4 \theta \sin \theta \, d\theta \quad u = \cos \theta \quad du = -\sin \theta \, d\theta \\ = \int -u^4 \, du = -\frac{1}{5} u^5 + C = \boxed{-\frac{1}{5} \cos^5 \theta + C}$$