

p. 33

2. $h = 58t - .83t^2$

a. i. $\frac{h(1) - h(2)}{1-2} = \frac{57.17 - 112.68}{1-2} = 55.5 \text{ m/s}$

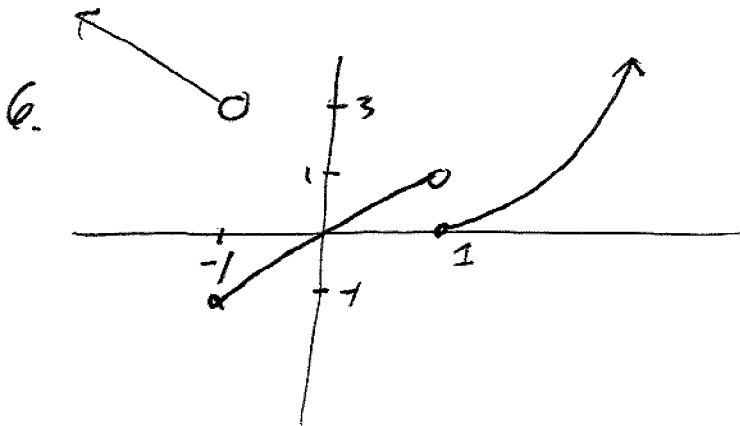
ii. $\frac{h(1) - h(1.5)}{1-1.5} = \frac{57.17 - 83.125}{-.5} = 55.925 \text{ m/s}$

(iii) $\frac{h(1) - h(1.1)}{1-1.1} = \frac{57.17 - 62.7937}{-.1} = 56.257 \text{ m/s}$

iv. $\frac{h(1) - h(1.01)}{1-1.01} = \frac{57.17 - 57.73317}{-.01} = 56.3317 \text{ m/s}$

v. $\frac{h(1) - h(1.001)}{1-1.001} = \frac{57.17 - 57.22633917}{-.001} = 56.3397 \text{ m/s}$

∴ I estimate 56.34 m/s



limit exists
except for $x = \pm 1$

12. Let $f(x) = \frac{x^2 - 2x}{x^2 - x - 2}$

$f(0) = 0$

$f(-.5) = -1$

$f(-.9) = -9$

$f(-.95) = -19$

$f(-.99) = -99$

$f(-.999) = -999$

$f(2) = 2$

$f(1.5) = 3$

$f(1.1) = 11$

$f(1.01) = 101$

$f(1.001) = 1001$

This limit does not exist!

13. $\lim_{x \rightarrow 0} \frac{\sin x}{x + \tan x}$ this function is even, so $f(x) = f(-x)$

$f(\pm 1) = .329$

$f(\pm .5) = .4582$

$f(\pm .2) = .49333$

$f(\pm .1) = .498333$

$f(\pm .05) = .499583$

$f(\pm .01) = .499983$

I guess limit is $1/2$

15. $f(x) = \frac{\sqrt{x+4} - 2}{x}$

x	f(x)
.1	.24845
.01	.24984
.001	.249984
-.001	.249984
-.0001	.250016

I guess $\lim_{x \rightarrow 0} f(x) = 0.25$

18. $\lim_{x \rightarrow 0} \frac{9^x - 5^x}{x}$

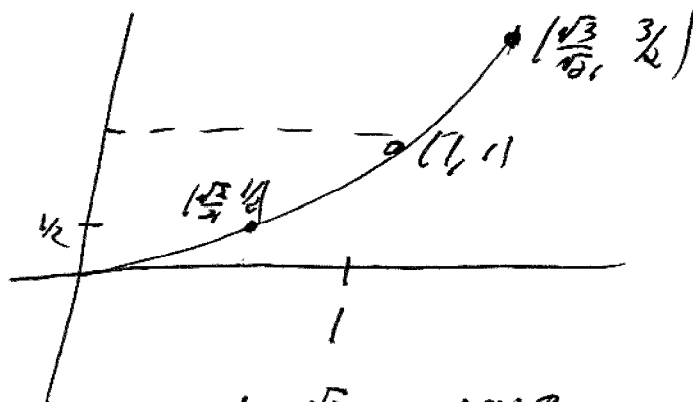
x	f(x)
.1	.711119
.01	.588002
.001	.587804
-.1	.4259
-.01	.5707
-.001	.5800024

$f(1.000001) = .58780006$

$f(-1.000001) = .5880000$

I guess $\lim \approx .588$

24.



$1 - \frac{\sqrt{2}}{2} \approx .2928..$

$\sqrt{3/4} - 1 = .224744..$

Choose $\delta = \sqrt{3/4} - 1$

(or any smaller #)

1.3

#30 $\lim_{x \rightarrow -2} (\frac{1}{2}x + 3) = 2$

Proof Let $\epsilon > 0$. Choose $\delta = 2\epsilon$. Suppose $0 < |x - (-2)| < \delta$
" $|x + 2|$

Then $|f(x) - L| = |\frac{1}{2}x + 3 - 2|$
 $= |\frac{1}{2}x + 1| = \frac{1}{2}|x + 2| < \frac{1}{2}\delta = \epsilon$

Thus $0 < |x - a| < \delta \Rightarrow |f(x) - L| < \epsilon$ as required. \square

#38 $\lim_{x \rightarrow a} c = c$

Proof Let $\epsilon > 0$. Choose $\delta = \epsilon$ (any δ works here!)

If $0 < |x - a| < \delta$ then $|f(x) - L| = |c - c| = 0 < \epsilon$ as required.

#44 $\lim_{x \rightarrow 3} x^2 + x - 4 = 8$

Proof

Let $\epsilon > 0$ be given. Choose $\delta = \min(1, \epsilon/8)$.

When $|x - 3| < 1$ then $|x + 4| < 8$. So for $0 < |x - 3| < \delta$ we have

$$|f(x) - 8| = |x^2 + x - 8| = |x + 4||x - 3| < 8|x - 3| < \epsilon \text{ as required!}$$

1.4

1. a. 5 b. 9 c. 2 d. $-\frac{1}{3}$ e. $-\frac{3}{8}$ f. 0 g. DNE, $\lim \frac{f}{g}$ rule only applies if $\lim g = 0$ h. $-\frac{6}{11}$ 2. a. 2 b. DNE, $\lim_{x \rightarrow 1} |g(x)| = \text{DNE}$ c. 0 d. DNE since $\lim_{x \rightarrow 1} |g(x)| = 0$

e. 16 f. 2

10a. $\frac{x^2+x-6}{x-2} = x+3$ does not hold when $x=2$ since we can't cancel $x-2$ then.

b. $\lim_{x \rightarrow 2} \frac{x^2+x-6}{x-2} = \lim_{x \rightarrow 2} x+3$

is still correct because $\frac{x^2+x-6}{x-2} = x+3$ for any x except $x=2$ and changing the function at $x=2$ does not change the limit!

18. $\lim_{h \rightarrow 0} \frac{\sqrt{1+h}-1}{h} = \lim_{h \rightarrow 0} \frac{1+h-1}{h(\sqrt{1+h}+1)} = \lim_{h \rightarrow 0} \frac{1}{\sqrt{1+h}+1} = \frac{1}{2}$

$$31. -1 \leq \cos\left(\frac{2}{x}\right) \leq 1 \quad \text{so}$$

$$-x^4 \leq \cos\left(\frac{2}{x}\right)x^4 \leq x^4$$

$$\text{and } \lim_{x \rightarrow 0} x^4 = \lim_{x \rightarrow 0} -x^4 = 0 \quad \text{so}$$

$$\lim_{x \rightarrow 0} x^2 \cos\left(\frac{2}{x}\right) = 0 \quad \text{by Squeeze Thm.}$$

$$34. \frac{2x+12}{|x+6|} = 2 \cdot \frac{x+6}{|x+6|} = \begin{cases} 2 & x > -6 \\ -2 & x < -6 \\ \text{DNE} & x = -6 \end{cases}$$

$$\text{Thus } \lim_{x \rightarrow -6} \frac{2x+12}{|x+6|} \text{ DNE}$$

$$43. \lim_{x \rightarrow 0} \frac{\sin 3x}{x} = \lim_{x \rightarrow 0} \frac{\sin 3x}{3} = 3$$