

Name: SOLUTIONS

Quiz #6 - February 16, 2007

1. $\int \cos^5 x \sin x dx$.

$$\begin{aligned} u &= \cos x \\ du &= -\sin x dx \end{aligned} = \boxed{-\frac{1}{6} \cos^6 x + C}$$

2. $\int \sin^2(x) dx$

$$= \int \frac{1}{2} - \frac{1}{2} \cos 2x dx$$

$$= \boxed{\frac{1}{2}x - \frac{1}{4} \sin 2x + C}$$

3. $\int \sec^3(x) \tan^3(x) dx$

$$= \int \sec^2 x \tan^2 x \cdot \sec x \tan x dx$$

$$= \int (\sec^2 x - 1) \tan^2 x \sec x \tan x dx$$

$$u = \tan x \quad du = \sec^2 x dx$$

$$= \int \sec^2 x (\sec^2 x - 1) \sec x \tan x dx$$

$$u = \sec x \quad du = \sec x \tan x dx$$

$$= \int u^4 - u^2 du = \frac{1}{5} u^5 - \frac{1}{3} u^3 + C$$

$$= \boxed{\frac{1}{5} \sec^5 x - \frac{1}{3} \sec^3 x + C}$$